Econometrics (Econ 452) – Fall 2022 – Instructor: Daniele Girardi

8 – PANEL DATA

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6. 131

SECTION 8 – PANEL DATA THE PLAN

- 1. Panel Data Structure.
- 2. Panel Data with Two Time Periods.
- 3. Fixed Effects Regression.
- 4. Time Effects & the TWFE model.
- 5. The Fixed Effects Model's Assumptions for Causal Inference.
- 6. Standard Errors in Panel Data.
- 7. Application: Drunk Driving Laws & Traffic Deaths.

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OVERVIEW: WHY PANEL DATA?

- Tracking multiple individuals over time
- Can compare *changes* in X & Y over time across units.
- Allows to control for (some)
 unobservable factors.
- But requires different ("clustered") standard errors.

	AMERICAN AIB	INDARY ULINES GROUP INC ULINES GROUP INC	year 2004 2005 2006 2007 2008 2009 2010 2011 2012 2012 2013	LTD 1.4e+08 1.3e+08 1.2e+08 1.0e+08 9.0e+07 1.1e+08 9.3e+07 6.7e+07 7.1e+07	EBIT 1.2e+07 1.3e+07 2.2e+07 2.1e+07 5.1e+06 2.6e+06 1.3e+07 7.0e+06	INT 7.3e+06 8.3e+06 9.4e+06 8.6e+06 6.9e+06 6.3e+06 7.4e+06			
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	11 AMERICAN AIR 12 PINNACLE WE 13 PINNACLE WE	LINES GROUP INC		1.5e+08	3.0e+07	7.1e+06			
	13 PINNACLE WE		2014	1.6e+08	6.6e+07	8.1e+06			
	13 PINNACLE WE		2004	2.6e+07	9.1e+06	1.9e+06			
		ST CAPITAL CORP	2005	2.6e+07	1.0e+07	1.8e+06			
		ST CAPITAL CORP	2006	3.2e+07	9.8e+06	1.5e+06			
	15 PINNACLE WE	ST CAPITAL CORP	2007	3.1e+07	9.9e+06	1.9e+06			
		ST CAPITAL CORP	2008	3.0e+07	9.20+06	242330			
	17 PINNACLE WE	ST CAPITAL CORP	2009	3.4e+07	9.8e+06	2.0e+06			
		ST CAPITAL CORP	2010	3.0e+07	1.1e+07	2.2e+06			
		ST CAPITAL CORP	2011	3.0e+07	1.2e+07	2.2e+06			
		ST CAPITAL CORP	2012	3.2e+07	1.3e+07	2.0e+06			
		ST CAPITAL CORP	2013	2.8e+07	1.3e+07	1.8e+06			
		ST CAPITAL CORP	2014	3.0e+07	1.2e+07	1.8e+06			
		TT LABORATORIES	2004	4.8e+07	5.7e+07	2.0e+06			
		TT LABORATORIES	2005	4.6e+07	6.2e+07	2.1e+06			
		TT LABORATORIES	2006	7.0e+07	6.4e+07	4.3e+06			
	26 ABB0	TT LABORATORIES	2007	9.5e+07	7.4e+07	5.6e+06			
		TT LABORATORIES	2008	8.7e+07	8.3e+07	5.6e+06			
		TT LABORATORIES	2009	1.1e+08	9.0e+07	5.1e+06			
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8.1 PANEL DATA STRUCTURE

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THREE TYPES OF DATA

Cross-Sectional.

- *"Screenshot" of different entities in a single time-period.*
- Time-Series.
 - A single entity followed for multiple timeperiods.
- Panel (or longitudinal)
 - Multiple entities followed for two or more time periods.





PANEL DATA

• *n* different entities, each observed at *T* different periods.

Notation:

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- *i* = one (generic) entity.
- *n* = *total* number of entities.
- *t* = one (generic) time period.
- *T* = total number of time periods.
- Y_{it} = variable Y for unit *i* at time *t*.
- $i = 1, ..., n \rightarrow$ the list of entities.
- $T = 1, ..., T \rightarrow$ the list of time periods.
- A panel dataset can be *balanced* or *unbalanced*.

Econometrics (Econ 452) -

	9					
Edit mo		Save Find				
	unit[1]		1			
	unit	time	Y	X1	X2	
1	1	1	202.5588	-19.22264	129.2636	
2	1	2	104.2631	-8.070382	125.4709	
3	1	3	29.77124	61.50526	147.9711	
4	1	4	-172.2132	-135.8765	-183.4996	
5	1	5	-72.91995	9.291389	-1.059095	
6	2	1	-61.89822	-130.0697	-77.89272	
7	2	2	-95.60616	-111.8378	-160.6753	
8	2	3	71.0319	-192.2037	86.28811	
9	2	4	-1.714685	-115.199	136.7121	
10	2	5	179.3087	117.5241	-86.32957	
11	3	1	208.0849	-136.4253	78.39323	
12	3	2	-65.77222	128.4241	79.56686	
13	3	3	3863547	-89.31672	-16.51904	
14	3	4	-33.60559	154.7801	-103.5521	
15	3	5	-226.0383	37.95787	-43.9291	
16	4	1	-70.60056	7.230512	-108.6402	
17	4	2	5.290823	150.3593	259.3312	
18	4	3	-29.76007	-74.51495	5.438204	
19	4	4	-21.65111	51.5759	-140.877	
20	4	5	129.9809	21.44303	11.02391	
21	5	1	-268.5881	-35.96759	56.76199	
22	5	2	-127.7903	-141.1225	38.18351	
23	5	3	-52.39587	29.19638	-8.14588	
24	5	4	86.98702	56.08614	-166.6773	
25	5	5	104.0118	73.22259	-169.8337	
26	6	1	-209.6827	-114.1686	240.1911	
27	6	2	-5.266198	-7.821132	226.6435	

A PANEL DATASET: TRAFFIC DEATHS AND ALCOHOL TAXES

Observational unit: a year in a U.S. state.

- 48 U.S. states $\rightarrow n = 48$
- 7 years (1982,..., 1988) $\rightarrow T = 7$
- Balanced panel, so total observations = $n \times T = 7 \times 48 = 336$

Variables:

- Traffic fatality rate (# traffic deaths per 10,000 state residents)
- Tax on a case of beer
- Other (legal driving age, drunk driving laws, etc.)

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Data Editor (Browse) — fatality.dta

	state[1]		1		
	state	year	beertax	vfrall	
1	AL	1982	1.539379	2.12836	
2	AL	1983	1.788991	2.34848	
3	AL	1984	1.714286	2.33643	
4	AL	1985	1.652542	2.19348	
5	AL	1986	1.609907	2.66914	
6	AL	1987	1.56	2.71859	
7	AL	1988	1.501444	2.49391	
8	AZ	1982	.2147971	2.49914	
9	AZ	1983	.206422	2.26738	
10	AZ	1984	.2967033	2.82878	
11	AZ	1985	.3813559	2.80201	
12	AZ	1986	.371517	3.07106	
13	AZ	1987	.36	2.76728	
14	AZ	1988	.346487	2.70565	
15	AR	1982	.650358	2.38405	
16	AR	1983	.6754587	2.3957	
17	AR	1984	.5989011	2.23785	
18	AR	1985	.5773305	2.26367	
19	AR	1986	.5624355	2.54323	
20	AR	1987	.545	2.67588	
21	AR	1988	.5245429	2.54697	
22	CA	1982	.1073986	1.86194	
23	CA	1983	.103211	1.80672	
24	CA	1984	.0989011	1.94611	
25	CA	1985	.095339	1.88128	
26	CA	1986	.0928793	1.94548	
27	CA	1987	.09	1.98966	le
28	CA	1988	.0866218	1.90365	

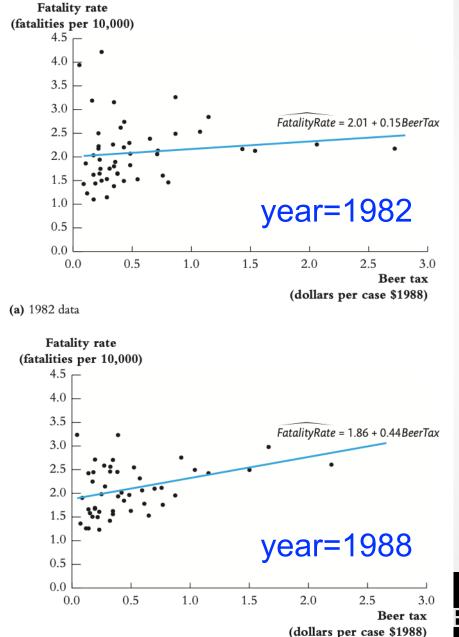
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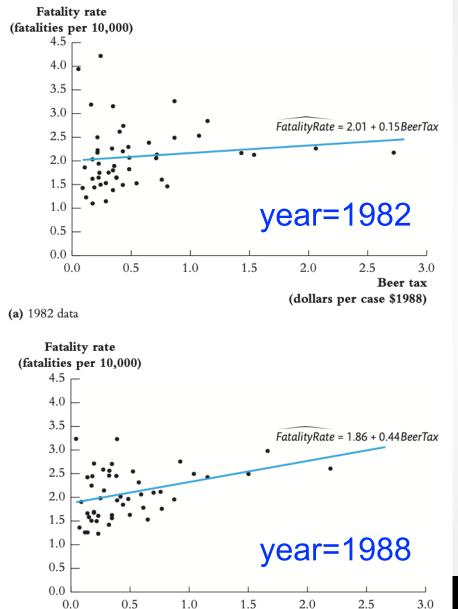
A PANEL DATASET: TRAFFIC DEATHS AND ALCOHOL TAXES

The dataset in STATA



A PANEL DATASET: TRAFFIC DEATHS AND ALCOHOL TAXES

- Consider a *cross-section* of the 48 States in a single year.
- In each single year, we can estimate $FatalityRate_{i} = \beta_{0} + \beta_{1}BeerTax_{i} + u_{i}$
- Higher alcohol taxes, more traffic deaths??



(dollars per case \$1988)

Beer tax

A PANEL DATASET: TRAFFIC DEATHS AND ALCOHOL TAXES

Why?

. . .

Some possible omitted factors:

- Income level.
 - Urban vs. Rural.
- Culture around alcohol & driving.
- Reverse causality.

PANEL DATA & FIXED EFFECTS

- Panel data allows to control for some omitted variables even without explicitly including them in the regression.
- Factors that are constant over time for a given unit
 → entity (or unit) fixed effects
- Factors that vary over time but are common to all units
 → time fixed effects



8.2 PANEL DATA WITH TWO TIME PERIODS

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PANEL DATA WITH 2 PERIODS

- Consider only the data for 1982 and 1988
- \rightarrow T=2.
- We can estimate a regression comparing *changes*:

 $\Delta FatalityRate_i = \beta_0 + \beta_1 \Delta BeerTax_i + u_i$

- with $\Delta X_i = X_{i1988} X_{i1982}$
- "Differenced" regression model
- Implicitly controls for all factors that vary across States but not over time.

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DERIVATION OF THE "DIFFERENCED" MODEL

• Assume that fatality rate in 1982 and 1988 is determined as

 $FatalityRate_{1982i} = \beta_{0,1982} + \beta_1 BeerTax_{i1982} + \beta_2 Z_i + u_{1982i}$

 $FatalityRate_{1988i} = \beta_{0,1988} + \beta_1 BeerTax_{i1988} + \beta_2 Z_i + u_{1988i}$

• Subtracting:

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 $\Delta FatalityRate_{i} = (\beta_{0,1988} - \beta_{0,1982}) + \beta_{1} \Delta BeerTax_{i} + (u_{1988i} - u_{1982i})$ $= \beta_{0} + \beta_{1} \Delta BeerTax_{i} + u_{i}$

• \rightarrow "Filters out" the effect of Z_i

THE "DIFFERENCED" MODEL IN GENERAL

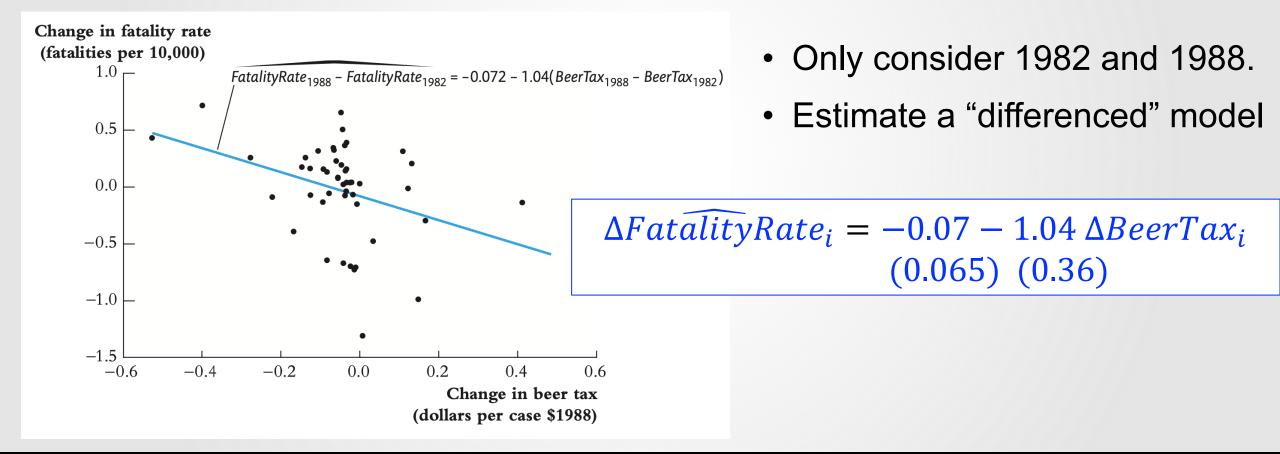
• In general, with T=2, the differenced model is

 $\Delta Y_i = \beta_0 + \beta_1 \Delta X_i + u_i$

• Statistical inference (SEs, hypothesis testing) is as usual.



A DIFFERENCED MODEL FOR THE EFFECT OF ALCOHOL TAXES



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8.3 FIXED EFFECTS REGRESSION

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THE FIXED EFFECT MODEL

 $Y_{it} = \alpha_i + \beta_1 X_{it} + u_{it}$

- $\circ \alpha_i$ = unit fixed effect (or unit-specific intercept)
- Can be used with any T>2.
- An equivalent way to represent it:

 $Y_{it} = \beta_1 X_{it} + \gamma_1 D 1_i + \gamma_2 D 2_i + \dots + \gamma_n D n_i + u_{it}$

$$D1_i = 1 \text{ for unit } 1 \text{ (}i=1\text{);}$$

= 0 for other units (i≠1).



THE FIXED EFFECT MODEL: DERIVATION

- Where does the fixed-effects model come from?
- Start from the following regression model:

 $Y_{it} = \beta_0 + \beta_2 Z_i + \beta_1 X_{it} + u_{it}$

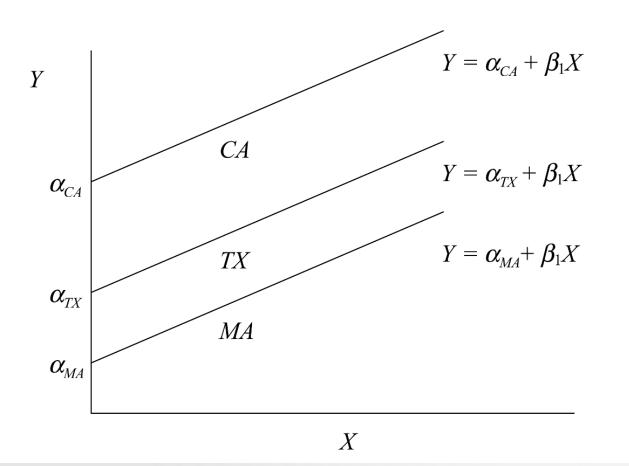
 \circ Z_i = unit-specific fixed variable.

- Define $\alpha_i = \beta_0 + \beta_2 Z_i$
- So we have:

 $Y_{it} = \alpha_i + \beta_1 X_{it} + u_{it}$



THE FIXED EFFECT MODEL



- Consider 3 states: CA, TX, MA.
- Their regression lines are: $\begin{aligned}
 \hat{Y}_{CA,t} &= \alpha_{CA} + \beta_1 X_{CA,t} \\
 \hat{Y}_{TX,t} &= \alpha_{TX} + \beta_1 X_{TX,t} \\
 \hat{Y}_{MA,t} &= \alpha_{MA} + \beta_1 X_{MA,t}
 \end{aligned}$

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PREVIOUSLY ON ECON 452...

- Panel data: *n* units over *T* periods.
- Differenced regression model (with T=2):

 $\Delta Y_i = \beta_0 + \beta_1 \Delta X_i + u_i$

• Fixed-effects model:

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 $Y_{it} = \alpha_i + \beta_1 X_{it} + u_{it}$

• Both control for any unobserved unit-specific fixed characteristic.

FIXED EFFECTS AS "DEMEANING"

Fixed-effects model

$$Y_{it} = \alpha_i + \beta_1 X_{it} + u_{it}$$

• Taking averages over time, this implies

 $\bar{Y}_i = \alpha_i + \beta_1 \bar{X}_i + \bar{u}_i$

• Subtract the 2nd equation from the 1st:

$$(Y_{it} - \overline{Y}_i) = \beta_1 (X_{it} - \overline{X}_i) + (u_{it} - \overline{u}_i)$$

- Defining $\tilde{Y}_{it} = Y_{it} \bar{Y}_i$ (& similarly for X and u): $\tilde{Y}_{it} = \beta_1 \tilde{X}_{it} + \tilde{u}_{it}$
- Takeaway:

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- The fixed-effects β_1 estimate can also be obtained by regressing "demeaned" Y on "demeaned" X, where "demeaned" means you subtract the unit-specific average.
- o In other words, we are taking both Y & X in deviations from unit-specific means.

ESTIMATING THE FIXED-EFFECTS MODEL

Two ways to estimate the fixed-effects model:

1. OLS regression with no intercept & n binary variables (D1, D2, ..., Dn):

 $Y_{it} = \beta_1 X_{it} + \gamma_1 D 1_i + \gamma_2 D 2_i + \dots + \gamma_n D n_i + u_{it}$

o It can also have a common intercept but n-1 indicators (as in the textbook).

2. OLS regression of "demeaned" variables:

 $\tilde{Y}_{it} = \beta_1 \tilde{X}_{it} + \tilde{u}_{it}$

• STATA xtreg command uses "demeaning".

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A FIXED EFFECTS MODEL FOR THE EFFECT OF ALCOHOL TAXES

We want to estimate β_1 in

 $FatalityRate_{it} = \alpha_i + \beta_1 BeerTax_{it} + u_{it}$

• How do we do it in STATA?



Data Editor (Browse) — fatality.dta

	state[1]		1		
	state	year	beertax	vfrall	
1	AL	1982	1.539379	2.12836	
2	AL	1983	1.788991	2.34848	
3	AL	1984	1.714286	2.33643	
4	AL	1985	1.652542	2.19348	
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22	CA	1982	.1073986	1.86194	
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24	СА	1984	.0989011	1.94611	
25	СА	1985	.095339	1.88128	
26	СА	1986	.0928793	1.94548	
27	СА	1987	.09	1.98966	K
28	CA	1988	.0866218	1.90365	
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A FIXED EFFECTS MODEL FOR THE EFFECT OF ALCOHOL TAXES

The dataset in STATA

A FIXED EFFECTS MODEL FOR THE EFFECT OF ALCOHOL TAXES

1. Let STATA know you are working with panel data

. xtset state year
 panel variable: state (strongly balanced)
 time variable: year, 1982 to 1988
 delta: 1 unit



. xtreg vfrall beertax, fe vce(cluster state)

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lixed-effects	(within) regr	ression		Number of	obs	=	336
Group variable:	state			Number of	groups	s =	48
R-sq: within	= 0.0407			Obs per g	roup: n	min =	7
between	= 0.1101				6	avg =	7.0
overall	= 0.0934				n	nax =	7
				F(1,47)		=	5.05
				Drah N E		=	0.0294
corr(u_i, Xb)	= -0.6885	(Std.	Err. ad	Prob > F justed for			
corr(u_i, Xb)	= -0.6885		Err. ad				
_ I	= -0.6885 Coef.	Robust		justed for	48 clus	sters	in state)
- vfrall		Robust Std. Err.		justed for P> t	48 clus	sters Conf.	in state) Interval]
- vfrall	Coef.	Robust Std. Err.		justed for P> t 	48 clus [95% C	sters Conf.	in state) Interval]

DIFFERENCED VS. FIXED-EFFECTS: COMPARING RESULTS

"Differenced" specification taking the 1982-1988 change:

 $\Delta FatalityRate_i = -0.07 - 1.04 \Delta BeerTax_i$

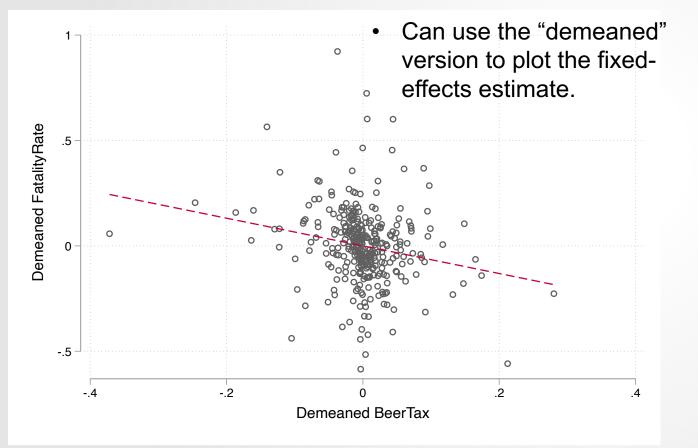
(0.065) (0.36)

• Fixed-effects specification:

 $FatalityRate_{it} = -0.66 BeerTax_{it} + State fixed effects$ (0.29)



SEEING THROUGH A FIXED EFFECTS REGRESSION



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STATA code:

- bysort state: egen avg_beertax=mean(beertax)
- bysort state: egen avg_vfrall=mean(vfrall)
- gen beertax_demeaned=beertax-avg_beertax
- gen vfrall_demeaned=vfrall-avg_vfrall
- twoway ///

(scatter vfrall_demeaned beertax_demeaned, ytitle("Demeaned FatalityRate") xtitle("Demeaned BeerTax")) /// (lfit vfrall_demeaned beertax_demeaned, estopts(noconstant) lcolor(cranberry)), scheme(plotplain) legend(off)

8.4 TIME EFFECTS AND THE TWFE MODEL

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TIME FIXED EFFECTS

- An omitted variable might vary over time but be common to all units.
 - Federal laws, innovations in car-making, ...
- Time fixed effects:

 $Y_{it} = \beta_1 X_{it} + \lambda_t + u_{it}$

• Estimated by introducing *T* binary variables:

 $Y_{it} = \beta_1 X_{it} + \delta_1 B \mathbf{1}_t + \delta_2 B \mathbf{2}_t + \dots + \delta_T B T_t + u_{it}$

where
$$B2_t = \begin{cases} 1 \text{ when } t=2 \text{ (year #2)} \\ 0 \text{ otherwise} \end{cases}$$
, etc.



TIME FIXED EFFECTS AS "TIME DEMEANING"

• Time fixed-effects model

$$Y_{it} = \lambda_t + \beta_1 X_{it} + u_{it}$$

• Taking time-averages across units, this implies

 $\bar{Y}_t = \lambda_t + \beta_1 \bar{X}_t + \bar{u}_{it}$

• Subtract the 2nd equation from the 1st:

$$(Y_{it} - \overline{Y}_t) = \beta_1 (X_{it} - \overline{X}_t) + (u_{it} - \overline{u}_t)$$

• Defining $\check{Y}_{it} = Y_{it} - \overline{Y}_t$ (& similarly for X and u):

 $\check{Y}_{it} = \beta_1 \check{X}_{it} + \check{u}_{it}$

• Takeaway:

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The time fixed-effects β₁ estimate can also be obtained by regressing "time-demeaned" Y on "time-demeaned" X, where "time-demeaned" means you subtract the time-specific average (=average of all observations for time t).

THE TWFE MODEL

- We usually want both unit & time fixed effects.
- Two Way Fixed Effects (TWFE) model:

 $Y_{it} = \alpha_i + \lambda_t + \beta_1 X_{it} + u_{it}$

- 3 equivalent ways to estimate it:
- 1. Include *n* unit-specific binary variables + T time-specific ones.
- 2. Subtract unit-specific averages from X & Y. Then regress demeaned Y on demeaned X, including T time-specific binary variables.
- 3. Subtract unit averages & time averages, and regress "doubly-demeaned" Y on "doubly-demeaned" X.

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A TWFE MODEL FOR THE EFFECT OF ALCOHOL TAXES

We want to estimate β_1 in

 $FatalityRate_{it} = \alpha_i + \lambda_t + \beta_1 BeerTax_{it} + u_{it}$

- How do we do it in STATA?
 - 'xtreg' + time-specific indicators, with "fe" option (option 1 & 2 in the following slides)
 - can also create the unit-specific and time-specific binary variables, and estimate a OLS regression (option 3 below).





. gen y83=(year==1983)

First generate all the time binary variables

- . gen y84=(year==1984)
- . gen y85=(year==1985)
- . gen y86=(year==1986)
- . gen y87=(year==1987)
- . gen y88=(year==1988)
- . global yeardum "y83 y84 y85 y86 y87 y88"
- . xtreg vfrall beertax \$yeardum, fe vce(cluster state)

Fixed-effects (within) regression	Number of obs = 336
Group variable: state	Number of groups = 48
R-sq: within = 0.0803	Obs per group: min = 7
between = 0.1101	avg = 7.0
overall = 0.0876	max = 7
$corr(u_i, Xb) = -0.6781$	Prob > F = 0.0009
(St	d. Err. adjusted for 48 clusters in state)
Robust	
vfrall Coef. Std. Err	t P> t [95% Conf. Interval]
++	
beertax 6399799 .3570783	-1.79 0.080 -1.358329 .0783691
y83 0799029 .0350861	-2.28 0.02715048690093188
y84 0724206 .0438809	-1.65 0.1061606975 .0158564
y85 1239763 .0460559	-2.69 0.01021662880313238
y86 0378645 .0570604	-0.66 0.5101526552 .0769262
y87 0509021 .0636084	-0.80 0.4281788656 .0770615
y88 0518038 .0644023	-0.80 0.4251813645 .0777568
_cons 2.42847 .2016885	i 12.04 0.000 2.022725 2.834215

Option 1: Create "manually" all time binary variables

Then run the fixed-effects regression using xtreg, including those binary variables.

ructor: Daniele Girardi

. xtreg vfrall beertax i.year, fe vce(cluster state)

AIIIIEISU

Fixed-effects Group variable	(within) regr e : state	ession		Number o Number o	fobs = fgroups =	336 48
R-squared:				Obs per	group:	
Within =	= 0.0803				min =	7
Between =	= 0.1101				avg =	7.0
0verall =	= 0.0876				max =	7
				F(7,47)	=	4.36
corr(u_i, Xb)	= -0.6781			Prob > F	=	0.0009
		(Std.	err. adj	justed for	48 clusters	in state)
		Robust				
vfrall	Coefficient	std. err.	t	P> t	[95% conf.	interval]
beertax	6399799	.3570783	-1.79	0.080	-1.358329	.0783691
year						
1983	0799029	.0350861	-2.28	0.027	1504869	0093188
1984	0724206	.0438809	-1.65	0.106	1606975	.0158564
1985	1239763	.0460559	-2.69	0.010	2166288	0313238
1986	0378645	.0570604	-0.66	0.510	1526552	.0769262
1987	0509021	.0636084	-0.80	0.428	1788656	.0770615
1988	0518038	.0644023	-0.80	0.425	1813645	.0777568

Option 2:

Run the fixed-effects regression using xtreg, **and** use the i. operator to let STATA generate the time-specific binary variables.

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. reg vfrall beertax i.state i.year, vce(cluster state)

Linear regression	Number of obs	=	336	
	F(6, 47)	=		
	Prob > F	=		
	R-squared	=	0.9089	
	Root MSE	=	.18788	

(Std. err. adjusted for **48** clusters in **state**)

vfrall	Coefficient	Robust std. err.	t	P> t	[95% conf	. interval]
beertax	6399799	.3857867	-1.66	0.104	-1.416083	.1361229
state						
AZ	5468622	.5064424	-1.08	0.286	-1.565693	.4719685
AR	6385298	.3986016	-1.60	0.116	-1.440413	.1633531
CA	-1.485192	.5892726	-2.52	0.015	-2.670655	2997283
С0	-1.461534	.5521075	-2.65	0.011	-2.572231	3508375
СТ	-1.840129	.5371107	-3.43	0.001	-2.920656	7596018
Amherst BE REVOLUTIONARY		5665606	-2.37.		<i>ๅ</i> &#^&#?</td><td><u>1/4/970</u></td></tr></tbody></table>	

Option 3: Use a OLS regression with both unit-specific & time-specific binary variables

8.5 THE FIXED-EFFECTS MODEL'S ASSUMPTIONS FOR CAUSAL INFERENCE

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ASSUMPTIONS FOR CAUSAL INFERENCE

TWFE Model: $Y_{it} = \alpha_i + \lambda_t + \beta_1 X_{it} + u_{it}$

Violated if there are lagged effects, where X_t affects not only Y_t but also Y_{t+1}

1.
$$E\left(\frac{u_{it}}{X_{i1}}, X_{i2}, \dots, X_{iT}, \alpha_i, \lambda_t\right) = E\left(\frac{u_{it}}{\alpha_i}, \lambda_t\right) = 0$$

- 2. $(X_{i1}, X_{i2}, ..., X_{iT}, u_{i1}, u_{i2}, ..., u_{iT})$ are i.i.d. across units
- 3. Large outliers are unlikely.
- 4. No perfect multicollinearity.

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8.6 STANDARD ERRORS WITH PANEL DATA

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CLUSTERED STANDARD ERRORS

• We assume observations are independent across different units.

○ → $u_{1982,CA}$ doesn't help predict $u_{1982,MA}$.

- We don't want to assume that observations belonging to the same unit are independent of one another.
 - autocorrelation: $u_{1982,CA}$ likely helps predict $u_{1983,CA}$
- **Clustered SEs** assume that variables are i.i.d across units but allow them to be *autocorrelated* within units.



CLUSTERED SEs IN STATA

. xtreg vfrall beertax, fe vce(cluster state)

U M Ar

Fixed-effects	(within) reg	ression		Number of o	bs =	336
Group variable	: state			Number of g	roups =	48
R-sq: within	= 0.0407			Obs per gro	up: min =	7
between	= 0.1101				avg =	7.0
overall	= 0.0934				max =	7
				F(1,47)	=	5.05
corr(u_i, Xb)	= -0.6885			Prob > F	=	0.0294
—						
		(Std.	Err. adj	usted for 48	clusters	in state)
I		Robust				
vfrall	Coef.	Std. Err.	t	P> t [95% Conf.	Interval]
+						
beertax	6558736	.2918556	-2.25	0.029 -1	.243011	0687358
_cons	2.377075	.1497966	15.87	0.000 2	.075723	2.678427

8.7 APPLICATION: DRUNK DRIVING LAWS & TRAFFIC DEATHS

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 TABLE 10.1
 Regression Analysis of the Effect of Drunk Driving Laws on Traffic Deaths

Dependent variable: tra	Dependent variable: traffic fatality rate (deaths per 10,000).												
Regressor	(1)	(2)	(3)	(4)	(5)	(6)	(7)						
Beer tax	0.36 (0.05) [0.26, 0.46]	-0.66 (0.29) [-1.23, -0.09]	-0.64 (0.36) [-1.35, 0.07]	-0.45 (0.30) [-1.04, 0.14]	-0.69 (0.35) [-1.38,0.00]	-0.46 (0.31) [-1.07, 0.15]	-0.93 (0.34) [-1.60, -0.26]						
Drinking age 18		0.10		0.03 (0.07) [-0.11, 0.17]	-0.01 (0.08) [-0.17, 0.15]		0.04 (0.10) [-0.16, 0.24]						
Drinking age 19				-0.02 (0.05) [-0.12, 0.08]	-0.08 (0.07) [-0.21, 0.06]		-0.07 (0.10) [-0.26, 0.13]						
Drinking age 20				0.03 (0.05) [-0.07, 0.13]	-0.10 (0.06) [-0.21, 0.01]		-0.11 (0.13) [-0.36, 0.14]						
Drinking age						0.00 (0.02) [-0.05, 0.04]							
Mandatory jail or community service?				0.04 (0.10) [-0.17, 0.25]	0.09 (0.11) [-0.14, 0.31]	0.04 (0.10) [-0.17, 0.25]	$\begin{array}{c} 0.09 \\ (0.16) \\ [-0.24, 0.42] \end{array}$						
Average vehicle miles per driver				0.008 (0.007)	0.017 (0.011)	0.009 (0.007)	0.124 (0.049)						
Unemployment rate				-0.063 (0.013)		-0.063 (0.013)	-0.091 (0.021)						
Real income per capita (logarithm)				1.82 (0.64)		1.79 (0.64)	1.00 (0.68)						
Years	1982–88	1982–88	1982–88	1982–88	1982–88	1982–88	1982 & 1988 only						
State effects?	no	yes	yes	yes	yes	yes	yes						
Time effects?	no	no	yes	yes	yes	yes	yes						
Clustered standard errors?	no	yes	yes	yes	yes	yes	yes						

Takeaways:

- Fairly large but imprecisely estimated effect of beer taxes.
- In the sample, average beer taxes are 0.50\$, and average fatality rate is 2.
- But with all controls, we can't reject the null of no effect at the 5% confidence level.
- Legal drinking age has no or little effect.
- Economic variables have large effects: good economy = more fatalities.

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ADDENDUM: THE DYNAMIC TWFE MODEL

- The assumption of *no lagged effects* is often unrealistic
 No lagged effects means that X_t affects only Y_t and not Y_{t+1}, Y_{t+2}, ...
- To allow for lagged effects, can use a *dynamic TWFE model*: $Y_{it} = \alpha_i + \lambda_t + \beta_0 X_{it} + \beta_1 X_{it-1} + \beta_2 X_{it-2} + \dots + \beta_m X_{it-m} + u_{it}$
- The β_0 , β_1 , β_2 , ..., β_m coefficients track the time path of the effect, allowing it to play out gradually over time.

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